

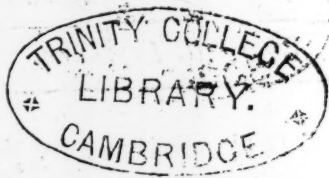
~~J. 227~~
Arithmetical ~~J. 14, 61~~
RECREATIONS:
OR, ~~Q. 13 a 4 b~~
ENCHIRIDION
OF
Arithmetical Questions:
Both Delightful and Profitable.

Whereunto are added
Diverse Compendious Rules in A-
rithmetick, by which some seem-
ing difficulties are removed, and
the performance of them rendred
familiar and easie to such as desire
to be Proficients in the Science of
NUMBERS.

All performed without ALGEBRA.

By Will. Leybourn.

LONDON: Printed by J. C. for
Hen. Brome and Sam. Speed. 1667.





To the ingenious
Student in the Sci-
ence of Numbers.

IN the perusal of several
Books, some of Vul-
gar, some of Decimal,
and some of Algebraical A-
rithmetick: as also of Geo-
metry, and other of the Sci-
ences Mathematical; in the
viewing and reading where-
of, when I met with any de-
A 2 light-

To the Studious

Wightful Arithmetical Question, which to resolve, required more then the common Rules of Vulgar Arithmetick do afford; I noted them down, which (together with diverse other, which at several times came into my thoughts) I have here heaped together, and bound them up in this small Enchiridion, or handful of Numerical Recreations, for the delight and exercise of such Youths and others, as are studious of, and desire to be Proficients in the Science of Numbers; Knowing, that by the practice and understanding the reason of these, and such like Questions (which will
not

READER.

not onely increase their knowledge in this Science, but recreate their spirits also) they shall with delight attain to a greater, and more then ordinary degree of knowledge in a short time, then by learning of Arithmetick, as (for the most part) it is now taught in Schools, in many Weeks. For, by the practising and right understanding of the reason of the resolving any few of these Questions, he shall accumulate to himself more profit in this Science, then by sitting at School two or three days; nay, (it may be) some weeks, Multiplie ing and dividing a great

To the Studious

number of Figures, which when he hath done (to his great loss of time) he knows not what he hath done nor, sometimes, he which putteth a Youth upon such harsh labour.

But I speak not this neither publish I this Manual, to the end it should be the onely Study and Practice of Youth; or to deter their Parents from putting them to School to learn Arithmetick, which is a Jewel fit to adorn all sorts and degrees of Men, from the highest to the lowest: but as useful Recreation, a spare hours, for Boys at School, to appose one another

READER.

another in; and at vacant times between their School-hours, to busie and delight themselves in. For what is more pleasing to Youth then Recreation? And what Recreation can he better make choice of, then that which will increase his knowledge?

We see by experience, that Man after Toyl and Labour desireth Rest, and after that returns again to his wonted employment, with the greater vigour and alacrity. And this is not experimentally true in Man only, but in other Creatures also, as may appear by that of the Poet.

To the Studious

A *Field* left fallow some
few years, will yeild

The richer Crops, when it a
gain is till'd :

A *River* stopped by a Sluce a
space,

Runs after rougher , and a
swifter pace :

A *Bow* a while unbent, will
after cast

Its Shafts the farther, and
them fix more fast :

A *Souldier* that a Season
still hath lain,

Comes with more fury to
the Field again.

Even so our *Body*, while
to gather breath,

From *Rest* to *Pain* again
it sojourneth ;

It

READER.

It recollects its Powers,
and with cheer
Falls fresh again into its
first career.

*For this, and the foremen-
tioned ends and purposes,
I have collected these fol-
lowing Numerical Recrea-
tions; in which, if thou
takest as much delight in
the practice of them, as I
have done in the composure,
thou shalt in the end finde thy
labour not lost, or (when
thou comest to years of di-
scretion) think thy time ill
spent.*

*The Questions are in num-
ber 40, intermixed one with
another, having no depen-
dance*

To the Studious

dance or coherence, every one proving it self without reference to any Rule, but what is to the Eye visible.

I could have made the number greater, but it would have been to no effect; for he that can work, and understand the reason of working these, may vary and make these 40 amount unto 400.

After the Questions, I have added diverse compendious Rules in Arithmetick, which will be of good use to such that have occasion to deal in the Multiplying and dividing of great Numbers, and for other purposes

READER.

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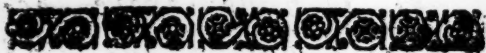
poses also. I might have added more, but these were such that at the present came into my minde, and, I think, they are such as are as necessary as any other I could have thought upon; I am sure they are as useful, and especially to those whose memories are not so quick and ready to Multiply and divide as some others are.

As I finde these accepted, I shall be the more animated to enlarge them, as occasion shall offer it self; in the mean time take this Treatise as it is, peruse it, and practice it, and if thou finde any thing

To the Studious, &c.
*thing to thy advantage,
make of it, and thank the E-
ditor.*

Vale.

Fare ever well, so ever
wishes he
Who is more thine, than he
can seem to be.



Arith-





Arithmetical
RECREATIONS:

Q. R.
Enchiridion, &c.

QUEST. 1.

*How to find the Number which
any person shall think up-
on, be it never so great.*

BId the party which
thinketh double his
thought, and multi-
ply that double by
5, and give you the
sum or product of
that Multiplication; from which
sum or product, if you omit the
last

last Figure thereof which standeth towards your right-hand (which will always be a Cypher) the remaining Figure or Figures shall be the number which the party thought upon.

Example :

Suppose the party should think upon 93, that doubled makes 186, which being multiplied by 5, the product will be 930; from which sum, if you omit the last Figure towards the Right-hand, (which is here a Cypher) the rest will be 93, the number which the party thought upon.

But because the last place being always a Cypher, may cause the other party which thinketh to conceive it easily, they being the very Figures which be thought remaining; it will be necessary (the more to obscure the

Recreations.

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and the business) to bid him adde to
and the last product some other num-
her, what you please, and then
ures let him give you the sum of all;
the from which, first subtracting the
number you bid him adde, and
then omitting the last Figure or
Cypher, the remainder then shall
also be the number which the
party thought at first.

Example :

Suppose a party should think
upon 297, this doubled will be
594, which being multiplied by
5, produceth 2970; to which
(the more to evade the business)
bid him adde 131, or any other
number, and then give you the
sum, which will then be 3101:
from which number, if you pri-
vately subtract the 131, which
you bid him adde, there will re-
main 2970, from which take the
Cypher,

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Cypher, and there will remain 297, the number which the party first thought upon.

QUEST. 2.

If two, three, four, or five persons should each of them think upon a several number, to tell what number each person thought upon, provided that none of the persons think above 9.

L Et the first party double the number he thought, and to that adde 5, and that sum multiply by 5, and to it add 10: From this number you privately substra^t 35, the first Figure of the remainder towards the left hand

Recreations.

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re hand shall be the number that
which the first party thought upon.
up

Example.

If the party think _____ 7
That doubled makes _____ 14
To which add 5, makes _____ 19
This 19 multiplied by 5, makes
_____ 95

To which add 10, it is _____ 105

From this 105 take 35, there
will remain 70, the first Figure
whereof is 7, the number
thought.

This you may do if one person
only think : but if two, three,
four or five persons think, it will
still be the same.

Example :

Let three persons, *William*,
James and *Thomas* think these
three Numbers, 4, 9 and 6.

William

6 *Arithmetical*

Williams number is _____ 4
Which bid him double, it makes _____ 8
To which let him add 5, it makes _____ 13
Which let him multiply by 5, it
produceth _____ 65
To this let him add 10, it
makes _____ 75

To this product let *James* pri-
vately add his number _____ 9
It makes _____ 84
Which let him multiply by 10,
it makes _____ 840

To this product let *Thomas*
privately add his number _____ 6
It makes _____ 846
Which let him multiply by 10,
it makes _____ 8460
This done, bid them give you
this last product, which is 8460 :
from this product 8460, do you
substract 3500, and there will re-
main

Recreations.

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main 4960; the Cypher being omitted, there will be left 4 9 6, which were the three numbers that the three parties thought.

Note, that if one party think, then you must take onely 35 from the last product: if two parties think, take 350; if three parties, take 3500; and if four parties, 35000, &c.

QUEST. 3.

A more artificial way to find the number that any person thinketh upon, without asking him any Questions.

L Et the party that thinketh multiply the number which he thought upon, by what number
ber

ber he pleaseth; then bid him divide the product of that multiplication, by what other number he pleaseth. Again, let him multiply this Quotient by what number he pleaseth, and divide that Quotient again, by what other number he thinketh fit; and let him thus continue multiplying and dividing as many or as few times as he pleaseth, either 2, 3, 4 or 5 times, or more or less at pleasure [*Onely so often as he multiplies and divides, let him tell you by what numbers he multiplies and divides.*] And when he hath multiplyed and divided as often as he listeth, bid him divide his last number by the number he thought upon, and keep the Quotient to himself.

In like manner do you take any number at adventure, and privately multiply and divide it as often as he doth, and by the same

Recreations.

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same number as he doth ; and
 when you have done it as often
 as he hath done , and divided
 your last number by the number
 that you supposed , you shall
 finde your last Quotient will be
 the same with his.

Then to know his number
 which he thought upon at first,
 bid him adde his last Quotient
 to the number which he thought
 upon , and give you the sum,
 from which sum subtract your
 last Quotient, and the number
 which he though upon will re-
 main.

Example :

Suppose a party should think up-
 on _____ 50

And multiply it by 4, it makes

_____ - 200 - 2

And divide that product by 5 it
 makes _____ 100

And multiply that Quotient a-
 gain

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gain by 6, it makes———600
And divide that again by 4, it
makes———150

And thus he may multiply and
divide, again and again, if
he pleaseth.

In the mean time, suppose you
should privately think upon--40
That multiplyed by 4, maketh
———160

And divided by 2, produceth--80
Which multiplyed again by 6,
giveth———480

And divided by 4, produceth
———120

Here you see that his last Quo-
tient is 150, which if he divide
by 50, the number which he
thought, the Quotient will be 3.

In like manner your last Quo-
tient is 120, which if you divide
by 40, (the number which you
supposed) your Quotient will be
also 3, equal to his. Now

Recreations. II

Now bid him add his last Quotient to his number thought, and give you the sum, which is 53; from which if you subtract your last Quotient 3, there will remain 50, the number which he first thought upon.

Again, this being a very delightful and pleasant Question, wherein there is couched much of the subtilty of numbers, I will not let it pass with one Example, but give you another.

Let the party think—————25
And multiply it by 8, makes--200
Divide that by 4, gives————50
That he multiplies by 3, gives
—————150
And divides it by 5, gives——30

This 30 being divided by 25,
his number thought, giveth
in the Quotient $1\frac{5}{5}$ or $1\frac{1}{5}$.

Now

12 *Arithmetical*

Now suppose you imagine — 30

And multiply that by 8, it makes

————— 240

And divide it by 4, it produceth

————— 60

Which multiplyed by 3, giveth

————— 180

This divided by 5, gives — 36

This 36 being divided by 30,
your number supposed,
giveth in the Quotient $1\frac{6}{10}$
or $1\frac{1}{5}$ equal to his last Quo-
tient.

Now if he add 25 his number
thought, to $1\frac{1}{5}$ his last number,
the sum will be $26\frac{1}{5}$; from which
if you take $1\frac{1}{5}$ your Quotient,
there will remain 25, the number
which he thought.

QUEST.

QUEST. 4.

If a Pile of Counters, or other pieces of money, or other things, lye on a heap together; and three parties take out from them a certain number unknown to you: by knowing the sum of them all, to finde how many each party took.

BId one of the parties take from the heap either 4, 8, 12, 32, 64, or any other number which may be divided by 4, and keep them to himself. Then say to the second party, For every four pieces that he hath, do you take seven pieces: And let the third party for every four pieces

B that

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that the first had, take 13 pieces ; which when they have done, bid them put them all together, and give you the sum ; which do you divide privately by 3, the Quotient shall be double to the number which the first party took.

Example: Suppose the first party took 12, that is three times 4 ; then the second person for every four must take 7, that is three times 7, or 21. Lastly, the third person must take three times 13, that is 39 : These three parcels being put together, make 72, which if you divide by 3, the Quotient will be 24, the half whereof is 12, the number of pieces that the first party took.

QUEST D
self

QUEST. 5.

Any number of Counters, Stones, Eggs, or other things being laid in a row, to tell what number any person, sitting by, thinketh upon, provided the party think not a number greater then the number of Counters, Stones, Eggs, &c. which lie before him.

L Et the nine ● following represent nine Counters, or the like.



Do you (privately to your self) call that which lyeth next
 B 2 your

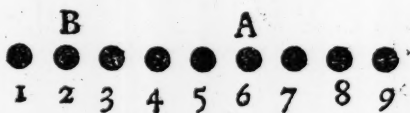
16 *Arithmetical*

your left hand One, the next Two, the third Three, &c. that then towards your right hand will be 9. Then bid any person think any number under 9, and pitch his finger upon which of the Counters he pleaseth: then (you knowing privately which Counter it is, whether the first, second, third, or any other) add 9 privately to that number; as if the party should lay his finger upon the sixth Counter, add 9 privately thereto, and it makes 15; therefore bid the party count to himself from that number which he thought, till he make it 15, and that Counter upon which the number 15 falleth, is the number which the party thought upon.

Example:

Example :

Let the nine Counters lye as
here you see.



Then suppose a party should
think upon 2, and that he should
pitch his finger upon the Coun-
ter noted with A, (which is the
sixth Counter.) Now (because he
pitched upon the sixth Counter)
add privately 9 to 6, and it will
make 15 : Wherefore, bid him
count from the number which
he thought upon (beginning at A
backwards, till he come to 15 ;
and his number will end at the
Counter B, which is the second
Counter, denoting that he
thought upon 2. For (being he
B 3 thought

thought upon 2) if he call the Counter A 2, the next Counter towards the left hand must be 3, the next 4, the next 5 ; and so the first Counter will be 7, then the last Counter will be 8, and the next to it 9 ; and so 15 will end at the Counter B, which is the second Counter, and denotes his number thought upon to be 2. And here note, that whereas here are onely 9 Counters placed, there might as well have been any other number, as 10, 12, 16, 20, 24, or any other number : only remember this, that whereas here you added 9 to the number of the Counters that the party pitched his finger upon, you then add that number which is equal to the number of Counters lying before you ; as if 10, then add 10 ; if 12, add 12 ; if 20, add 20, &c.

This is the way by which some wil

Recreations. 19

will dispose the several spots of the Cards, and lay them with the face downwards in order of a Dyal, counting the Ace 1, the Duce 2, the Tray 3, &c. the Queen 11, and the King 12: by which they will undertake to tell what hour you think upon; which is very pleasant to practise, and seeming strange to those who know not the reason of it.

B 4 QUEST.

QUEST. 6.

One person having two Bottles of Wine, in each hand one, the one being Sack, and the other Claret, (or any other two things, as two pieces of Money, &c. provided the one be even and the other odd) to finde in which hand the Bottle of Sack is, and in which the Claret; or in which hand the odd, and in which the even piece of money is.

L Et any person have in his hands two Bottles, one full of Sack, the other full of Claret; how

how to know in which hand he hath the Sack, and in which the Claret; to effect it, do thus:

Bid the partie that hath the Bottles in his hands to double the price of the Wine which he hath in his left hand, and treble the price of that Wine which he hath in his right-hand; then bid him add both numbers together, and ask him whether it be even or odd: if it be even, the Sack (or even piece of money) is in the right hand; but if it be odd, the Claret (or odd piece of money) is in the right-hand.

Example: -

Let one have a Bottle of Sack (or 12 *d.*) in his left hand, and a Bottle of Claret (or 5 *d.*) in his right-hand; he having thus disposed them unknown to you, bid him double the money in his

B 5

right-

right-hand, it is 24; then bid him treble the piece which is in his left-hand, and it is 15; then bid him add them both together, and they make 39: for 24 and 15 is 39. This done, ask him whether the number be even or odd. He will say, Odd. Then tell him he hath the Sack or 12 *d.* in his left hand, and the Claret or 5 *d.* in his right.

Or if he had had the Sack in his left-hand, and the Claret in his right, and you had said, Double that in your right-hand, it makes 10, and treble that in your left, it makes 36; add them together, they make 46; it being even, denotes the Claret or odd number to be in the right-hand. Wherefore observe this always:

If you double the right-hand,
and the number be even, the
odd

Recreations. 23

odd number is in the right. If you double the right-hand, and the number be odd, the even number is in the right.

If you treble the right-hand, and the number be even, the even number is in the right. If you treble the right-hand, and the number be odd, the odd number is in the right.

This may be done by two parties, interchanging two pieces of money, or by giving two persons two Cards, one odd, the other even; and placing them before you, that you suppose one to be the right-hand, and the other the left.

QUEST.

QUEST. 7.

A man being 100 years of age, upon his birth-day had his three sons with him at dinner, namely, William, James and Thomas: the Father saying to them, Well sons, I am this day just 100 years old; The youngest son, William, said, Father, my brother Thomas is four times as old as I am, and my brother James is three times as old as I am, and all our ages together are just 100 years. How old was each of the three sons?

TO resolve this, say, *William* was one year old; then *James* must

Recreations. 25

must be three times his age, that is three years old; and *Thomas* must be four times his age, that is four years old: now all these added together make but eight years, whereas they should be 100 years: Wherefore, divide 100 by 8, and the Quotient will be $12\frac{1}{2}$, that is 12 years and an half for the age of *William*. Then,

Years. Months.

William being 12——6

James must be 37——6 Three times as much, and

Thomas must be 50——0 Four times as much:

—————
In all 100——0 Equal to the Fathers age.

QUEST.

QUEST. 8.

A man dies, and leaves a Legacie of 900 l. to be disposed of among four of his relations, viz. A, B, C, and D; which Legacie is to be disposed of in this order; B is to have twice as much as A, and C thrice as much as B, and D is to have as much and half as much as C: what must each person have?

TO effect this, or the like, suppose that A were to have 1 l. then B must have 2 l. which is twice as much; and C must have 6 l. which is three times as much

Recreations.

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much as B; and D must have 9 l. which is as much and half as much as C.

These numbers added together make 18 : divide 900, the whole Legacie, by 18, the Quotient will be 50 l. for A, then B must have 100 l. and C 300 l. and D 450 l. which all being added together, make 900 l. equal to the whole Legacie, and so disposed according to the donors will, as by the work following may appear.

			l.
A	1	4	50
B	2	888	100
C	6	888	300
D	9	8	450
<hr/>			<hr/>
18			900

QUEST.

QUEST. 9.

*A man dies and leaves 3000 l.
to be distributed to his
Wife, his Son, and his
two Daughters in this wise;
That the Sons Portion
should be double to that of
the Mother, and the Mo-
thers Portion double to
each of the Daughters.
How much must each of
their Portions be?*

Suppose the Portion of one of
the Daughters to be 1 l.
then the Mothers Portion must
be double to one of the Daugh-
ters, (or equal to them both)
namely 2 l. and the Sons Por-
tion must be double to the Mo-
thers,

Recreations. 29

thers, namely 4 l. These four Portions added together, make 8 l. (as in the Example is expressed) but they should be equal to 3000 l. Wherefore divide 3000 by 8, and the Quotient will be 375 l. for one of the Daughters Portions: Then the Mothers istwice as much, namely 750 l. and the Sons double to that, namely 1500 l. All which is visible by the following Work.

l.

One Daughter	—	1	
The other Daughter	—	1	84 l.
The Mother	—	2	3000 (375
The Son	—	4	888

The sum — 8

One Daughter	—	375
The other Daughter	—	375
The Mother	—	750
The Son	—	1500

The sum — 3000

QUEST.

QUEST. 10.

There were in company together four persons, Adam, Edward, Charles, and William.--Adam told Edward that he was older then him by two years: Charles told them that he was as old as both of them together, and four years over.-- William hearing them say so, said to them, I am just 96 years old, and that is equal to all your ages. Now how old was Adam, Edward, and Charles severally?

SUPPOSE Edward were 1 year old, then Adam for Edward's

Recreations.

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wards age put (1), then *Adams* age must be (1 more by 2); and *Charles* his age must be (2 more by 6): These three ages added together in this manner, as is here expressed:

<i>Edward</i>	—	1	
<i>Adam</i>	—	1	more by 2.
<i>Charles</i>	—	2	more by 6.
4 more by 8.			

This 4 more by 8 should be equal to 96, *Williams* age, had your supposition been right; but being it is not, take 8 out of 96, and there will remain 88; which divide by 4, and the Quotient will be 22, which is *Edwards* age.— Then according to the Question, *Edward* being 22 years old, *Adam* must be 24 years old, which is as old as *Edward*, and 2 years more: then *Charles* must be

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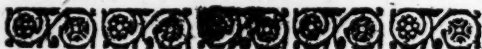
be 50 years old, which is as old as *Edward* and *Charles* together, and 4 years over. So all their ages added together, make 96 years, equal to *Williams* age, as here appeareth.

Edward ————— 22

Adam ————— 24

Charles ————— 50

—————
Williams age — 96



QUEST.

QUEST. II.

Three Persons, Andrew, Benjamin and Charles are to go a Journey of 235 Miles; of this Journey, Andrew is to go a certain number of Miles unknown; Benjamin is to go four times as many Miles as Andrew, and three Miles more; and Charles is to go twice as many Miles as Benjamin, and five Miles more. How many Miles must each of these persons travel severally, to make out their Journey 235 Miles?

Suppose that Andrew went only one Mile; then Benjamin must

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must go four times as much, that is, 4 Miles, and 3 over: Then *Charles* must go twice as much as *Benjamin*, which is 8 Miles, and 5 over. These numbers added together, as here you see, make but 13 Miles, and 8 over: Whereas the sum of all their journey should be 235 Miles.

Andrew travelled 1 Mile.

Benjamin travelled 4 Miles, and 3 over.

Charles travelled 8 Miles, and 5 over.

The sum ——— 13 Miles, and 8 over.

Wherefore, because your supposition was not right, subtract the 8 over-Miles from 235 (the number of Miles they were to go in all) and the remainder will be 227; divide 227 by 13, and the

Recreations. 35

hat the Quotient will be $17\frac{6}{3}$, so that
 hen *Andrew* for his share must travel
 n as 17 Miles, and $\frac{6}{3}$ of a Mile. And
 and *Benjamin* must travel 4 times as
 ded much, which is $68\frac{24}{3}$, and 3 Miles
 ke more; and *Charles* must go twice
 er: as far as he, which is $136\frac{48}{3}$, and
 ihr 3 Miles more. All which being
 added together, will make 235
 Miles; as you may here see.

d 3	<i>Andrew</i> must go—	$17\frac{6}{3}$	
	<i>Benjamin</i> —	$68\frac{24}{3}$	more 3
d 5	<i>Charles</i> —	$136\frac{48}{3}$	more 5
		<hr/>	
	The sum—	$221\frac{78}{3}$	more 8

d 8
 Here the sum is 221 Miles, and
 $\frac{78}{3}$, which makes just 6 Miles, and
 the 8 Miles more makes 235,
 which answers the Question.

QUEST.

QUEST. 12.

The Captain, Lieutenant and Cornet of a Troop have taken amongst them from some Enemy 478 Crowns, which they agree to share in this manner: The Captain is to have 24 times as much as the Cornet, wanting onely 7 Crowns, and the Lieutenant is to have 5 times as much as the Cornet, wanting 3 Crowns. I demand how much the Cornet must have, and consequently the Lieutenant and Captain?

IMagine the Cornet to have onely 1 share, it matters not what;

Recreations.

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what : then the Lieutenant must have 5 shares, wanting 3 Crowns ; and the Captain must have 24 shares, wanting 7 Crowns : Add all these shares together, as here you see.

The Cornet	1 share.
The Lieutenant	5 shares wanting 3 Crowns.
The Captain	24 shares wanting 7 Crowns.

The sum is 30 shares wanting 10 Crowns.

This 30 shares wanting 10 Crowns should be equal to 478 : but being it is not, add the 10 Crowns to 478, and it makes 488 ; which divide by 30 (the sum of the shares) and the Quotient will be $16\frac{8}{30}$ or $1\frac{4}{15}$, which is the Cornets share. Then the Lieutenants will be $77\frac{20}{15}$, which is

C

38 *Arithmetical*

is 5 times as much as the Cornets, wanting 3 Crowns; and the Captain must have $377\frac{96}{15}$, which is 24 times the Cornets share wanting 7 Crowns; and these three sums added together, make $470\frac{120}{15}$; as in the Example.

The Cornet	$16\frac{4}{15}$
The Lieutenant	$77\frac{20}{15}$
The Captain	$377\frac{96}{15}$

The sum $470\frac{120}{15}$

The Fractions make up shares, (which you may finde by dividing 120 by 15) which 8 being added to 470, maketh 478 the just sum to be shared.

QUEST

QUEST. 13.

A Drover driving of Sheep, one meets him, says, Good speed friend with thy 20 Sheep. Nay, says the Drover, I have not 20 Sheep, but had I as many more, and half as many more, and two Sheep and half a Sheep, then I should have 20 Sheep. How many Sheep had he in his Drove?

Suppose he had 1 Sheep, then as many more is 1, and half as many more is half a Sheep; that is 2 and an half; and 2

C 2

Sheep

40 *Arithmetical*

Sheep and an half more; add these together, thus:

1 Sheep.
 1 as many more.
 $\frac{1}{2}$ half as many more.
 more $2\frac{1}{2}$ Sheep

The sum $2\frac{1}{2}$ more by $2\frac{1}{2}$.

This $2\frac{1}{2}$ more by $2\frac{1}{2}$ should be equal to 20, but it is too little wherefore, take $2\frac{1}{2}$ from 20, and there will remain $17\frac{1}{2}$; which $17\frac{1}{2}$ being divided by $2\frac{1}{2}$, produceth in the Quotient 7: wherefore he must have 7 Sheep in his Drove.

7 Sheep.
 7 as many more.
 $3\frac{1}{2}$ half as many more
 more $2\frac{1}{2}$ Sheep.

$17\frac{1}{2}$ more $2\frac{1}{2}$ is equal to 20 which was required.

QUEST

QUEST. 14.

There is 273 l. to be divided amongst
4 Persons; namely, Andrew, Ben-
net, Christopher and Daniel.---

Andrew is to have a share un-
known. Bennet is to have twice as
much as Andrew, and 30 l. more.

Christopher is to have 3 times as
much as Andrew, wanting 52 l.

And Daniel is to have 5 times as
much as Andrew, and 20 l. more.--

How must this 273 l. be divided
amongst them, that every one have
his true share?

Share.

Suppose Andrew to have 1 for
his part.

Then Bennet must have 2, and
30 l. over.

And Christopher must have 3, lack
52 l.

And Daniel must have 5, and
20 l. over.

The sum of the shares is 11, lack
2 l.

C 3

The

The reason why I say 11 shares wanting 2 l. is because Bennet and Daniel together have 50 l. over, and Christopher wants 50 l. of 3 shares: therefore take their 50 l. from his 52 l. and there want only 2 l.

These 11 shares wanting 2 l. (by the tenor of the Question) should be equal to 273: but because 2 l. is wanting of eleven shares, therefore add 2 l. to 273 l. and it will be 275 l. which these 11 shares should be equal to; but being it is not, therefore divide 275 by 11, and the Quotient will be 25 l. for Andrews share. Then,

Andrews

Recreations: 43

Andrews share being ———— 25
 Bennets must be as much }
 more, which is 50 l. } 80
 and 30 l. more, in all }

And Christophers share must }
 be three times as much }
 as Andrews; that is 75 l. } 23
 wanting 52 l. that is — }

And Daniels must be 5 }
 times Andrews, which }
 is 125 l. and 20 l. more, } 145
 in all ———— }

The sum of the shares ———— 273

Which is equal to the sum to
 be divided, and is divided ac-
 cording to every punctilio of the
 Question.

C 4 QUEST.

QUEST. 15.

A Master agrees with a Servant to work with him 30 days, agreeing to give him for every day that he wrought 7 s. and for every day that he idled, the Servant was to abate 5 s. At the expiration of the 30 days, they come to an account, that the Master and Servant were both even, neither to receive any thing. How many days did the Servant work? and how many did he play?

Suppose I D, for the days he laboured, comes to ——— 7 s.
Then he idled 29 days, which comes to ——— 145 s.
Now

Recreations. 45

Now (because the money that his labour came to, and the money that he lost by neglect, came to the same; - therefore add 5 s. (which he was to allow every day he neglected) to both the above-supposed numbers, and they make 12 and 150: therefore divide 150 by 12, and you shall have in the Quotient $12\frac{1}{2}$, and so many days he laboured; which being subtracted from 30, the whole number of days, there remains $17\frac{1}{2}$, for the days he idled; for 12 days and an half, at 7 s. a day, comes to 4 l. 7 s. 6 d. also 17 days and an half which he idled, at 5 s. a day, comes to the same sum; which declares the work to be true.

C ; QUEST.

QUEST. 16.

A Dog is pursuing of a Hare, which is 100 yards before him; and for every yard that the Hare runs, the Dog runs two yards and an half (that is, the Dog runs two times and an half swifter than the Hare.) I would know how many yards the Hare hath run when the Dog overtaketh her?

PUt for the yards (1 Y) (or any other Mark or Letter;) therefore the yards are (100 more 1 Y;) and because the Dog runs twice and an half faster then the

the Hare, take any two numbers in like proportion, as $2\frac{1}{2}$ is to 1, which will be 5 and 2, (for 1 doubled makes 2, and $2\frac{1}{2}$ doubled makes 5 :) these numbers thus found, there is the same proportion between (100 more 1 Y) to (1 Y) as there is between 5 and 2 : Wherefore multiply (100 more 1 Y) by 2, the product is (200 more 2 Y) which is equal to (1 Y and 5 :) wherefore, if you subtract 2 from 5, there will remain 3 ; and divide 200 by 3, the Quotient will be $66\frac{2}{3}$. Therefore I say, that the Hare will have run 66 yards and $\frac{2}{3}$ of a yard (which is 2 foot) when the Dog shall have overtaken her ; and the Dog will have run $166\frac{2}{3}$ yards, which is twice and an half more than the Hare, for twice $66\frac{2}{3}$, and $33\frac{1}{3}$, which is half $66\frac{2}{3}$ is equal to $166\frac{2}{3}$, the quantity that the Dog ran.

QUEST.

QUEST. 17.

There are two Messengers set out from two Towns, which are 140 Miles asunder, upon one and the same day: The one travels 8 Miles a day, and the other 6 Miles. I demand how many days it will be ere they meet together.

Put one D (or day) for the time they shall meet; in which time the one would have travelled but 8 Miles of the Journey, and the other but 6 Miles; these added together, make but 14 Miles; whereas they should have travelled 140 Miles: divide therefore

Recreations.

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herefore 140 by 14, and the Quotient will be 10; so that in 10 days they will meet together: which may thus be proved.

He that travels 8 Miles a day, will in 10 days have travelled 10 times 8 Miles, that is 80 Miles. And

He that travels but 6 Miles a day, will in 10 days travel 6 times 10 Miles, that is 60 Miles

These two numbers, 60 and 80, being added together, make 140 Miles, equal to the distance of the two Towns.

QUEST.

QUEST. 18.

A Foot-man goes a Journey undertaking to go every day nine Miles : when he had been gone 10 days more expedition was required, and a Horse-man is sent after him. How many Miles in a day must the Horse-man ride to overtake the Foot-man in 18 days?

FOR the Miles that the Horse-man is to ride, suppose one part of the Journey, (or 1 M :) therefore in 18 days he would have travelled 18 M. Now for that the Foot-man travelling every day 9 Miles, he went in 18 days

Recreations. 51

ays 162 Miles; to the which add
0 Miles, which he went in the
0 days that he set out before
he Horse-man, and the sum is
52 Miles. Now if you divide
52 by 18 M, you shall have in
the Quotient 14: And so many
Miles must the Horse-man tra-
vel in a day, to overtake the Foot-
man in 18 days. --- For if you
multiply 18 by 14, the product
will be 252, equal to the Miles
the Foot-man travelled in 28
days.

QUEST.

QUEST. 19.

One buys 100 Turkeys for 17 pound, in the selling of which again, he loseth 18 pound in his laying out of 102 pound. I would know how many Turkeys be sold for one pound.

I Magine that he sold one Turkey for one pound: Then work by the Rule of Three, thus:

If 17 *l.* buy 100 Turkeys, how many will 102 *l.* buy?

Multiply 102 by 100, and the product will be 10200, which divide by 17, and the Quotient will be 600.

Then

Recreations. 53

Then say again by the Rule of Three,

As 1 *l.* is to 1 T. so is 102 *l.* wanting 18 *l.* which he lost, that is, 84 *l.* to 84.

Here the determination of the Question will be between 600, the first Quotient, and 84 the last Quotient.

Divide therefore 600 by 84, and the Quotient will be $7\frac{1}{3}$ T: and so many Turkeys he sold for one pound.

It may thus be proved by the converse working: For,

If $7\frac{1}{3}$ Turkeys cost 1 *l.* what will 600 Turkeys cost? Multiply and divide, you will find 84 *l.* which is 18 *l.* less then 102 *l.* which he laid out.

QUEST.

QUEST. 20.

One bought 8 yards of two sorts of Stuff, as Calico and Tammy, for 20 s. the Tammy cost 4 s. a yard, and the Calico 2 s. How many yards did he buy of each sort?

TO answer this, or the like Question, multiply 8 (the whole number of yards) by 2 (the least price) it produceth 16, which subtract from 20 (the whole price) the remainder will be 4, which divide by 2, (the difference of the price,) and the Quotient will be 2 for the number of yards of Tammy, and

Recreations. 55

and then there must be 6 yards
of Calico. For,

2 Yards of Tammy at 4 s. is
_____ 8 s.

And 6 Yards of Calico at 2 s. is
_____ 12 s.

In all _____ 20 s.

QUEST.

QUEST. 21.

There are four sorts of Money, of which of one sort 7 pieces makes a pound Sterling: Of the second sort, 18 pieces makes a pound: Of the third sort, 21 pieces makes a pound: And of the fourth sort, 28 pieces makes a pound. Of each of these pieces, a Merchant received in exchange a like number, all of them making 568 pound Sterling. I demand how many pieces there were in all? and how much money he had of each several piece?

PUt (or imagine) 1 P, for the quantity of each several sort

of

of Mony. Now because to a pound Sterling there went 7 pieces of the first, apply your self to the Rule of Three in this manner, saying,

If 7 pieces of Mony be worth 1 P.

If 7 P be worth 1 l. what is 1 P worth? The answer will be, $\frac{1}{7}$ of a pound. Then again,

If 18 P be worth 1 l. what is 1 P worth? Answer, $\frac{1}{18}$ of a pound. Again for the third sort,

If 21 P be worth 1 l. what 1 P? Answer, $\frac{1}{21}$ of a pound.

Lastly, if 28 P be worth 1 l. what 1 P? Answer, $\frac{1}{28}$ of a pound.

Now these Fractions do make together $\frac{71}{252}$, which should be equal to 568. But seeing it is not, divide therefore 568 by $\frac{71}{252}$, and you shall finde 2016, which is the value of 1 P: and so many of each

58 *Arithmetical*

each of the pieces he was to receive to make up his sum of 568 ^{l.} Sterling, which may be easily thus proved.

If 7 pieces are worth ——— 1
 What are 2016 worth? —288
 If 18 pieces are worth ——— 1
 What are 2016 worth? —112
 If 21 pieces are worth ——— 1
 What are 2016 worth? —96
 If 28 pieces are worth ——— 1
 What are 2016 worth? —72

Here you see, that
 2016 of the first pieces make--288
 As many of the second ——— 112
 As many of the third ——— 96
 And as many of the last ——— 72

Which added together, make-568
 Equal to the Mony changed, and
 so is the Question answered.

QUEST.

QUEST. 22.

There is an Army, whose Foot are 8 times the number of the Horse: Amongst them there is 392000 Dollers to be distributed; so that each Horse-man is to have 16 Dollers, and each Foot-souldier 5 Dollers. I demand, of how many Horse and how many Foot the whole Army consisted?

Imagine the Horse-men to be one, or (1 H).

And the Foot to be eight, or (8 F) because they are, (according to the Question) to be 8 times as many as the Horse. Now (because each Horse-man

is to have 16 Dollers) multiply
 16 by 1 H, and it makes 16 H
 Likewise, because each Foot-man
 is to have 5 Dollers, multiply
 5 by 8 F, and it makes 40 F
 add 16 H and 40 F together, the
 make 56, which should be equal
 to 392000 Dollers; but being
 is not, divide 392000 by 56, and
 the Quotient will be 7000, for
 the number of Horse-men; and
 that multiplied by 8, gives
 56000, for the number of Foot-

Now if you multiply 7000 by
 16, the product will be 112000
 for the number of Dollers to be
 distributed to the Horse-men
 and multiplying 56000 by 5, the
 product will be 280000 for the
 number of Dollers that the Foot-
 men are to have; and these
 two added together, make
 392000, equal to the number of
 Dollers to be distributed, and an-
 swers the Question in all its par-
 ticulars.

QUEST

QUEST. 23.

An Hegler goes to a Country-Market & buys 100 Eggs, which is 120) after the rate of 3 for a penny. At another Market he buyes 120 more at the rate of 2 for a penny ; these Eggs he mingles together, and sells his 240 Eggs at another Market after the rate of 5 Eggs for two-pence. I demand, whether he lost, gain'd, or saved by this bargain?

A Ccording to common acceptance, any person unacquainted with Arithmetick, would conclude that (besides his

D

Jour-

62 *Arithmetical*

Journeying from Market to Market) he lost nothing, nor gained nothing. But by Arithmetical proof, you shall find that he lost not only his Travel, but Money also.

For, by the common Rule of Three, you shall find, That if 3 Eggs cost one penny, 120 will cost 3*s.* 4*d.* for divide 120 Eggs by 3 Eggs, and there will be in the quotient 40 pence, which is 3*s.* 4*d.*

Likewise, by the same Rule, you shall find, That 120 Eggs at 2 for a penny, will come to 5*s.* for divide 120 by 2, and the quotient will be 60 pence, or 5*s.*

So that these two sums, *viz.* 3*s.* and 4*d.* and 5*s.* do make together 8*s.* and 4*d.* and so much did his 240 Eggs cost him at both Markets.

But

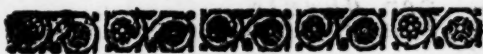
Recreations.

63

But now to see whether he gained or lost: Say by the same Rule of Three;

If 5 Eggs cost 2 pence, what shall 240 cost?

Multiply 240 by 2, it produceth 480, which divide by 5, and in the quotient you shall find 96 pence, which is but 8 shillings: So that besides all his Travel, he lost 4 pence in Money.



D 2

QUEST.

QUEST. 24.

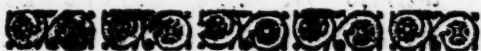
One comes to a Draper, and demands the Price of a yard of Canvas; the Draper demands 12 d. Says the Chapman, I will willingly give you Two shillings for every yard I buy of you; provided, that every Angel of my Money may go for Twenty shillings: To which the Draper Assents.

THis is rather a Fallacy than any thing else; but I have here inserted it, to shew the cunning reach of some persons, over the honest meaning of others.

The

Recreations. 65

The Draper and Chapman having thus agreed, the Chapman bids the Draper cut him off Five yards, which at 2 s. the yard comes to 10 s. The Chapman throws him down an Angel, (which by their agreement was to go for Twenty shillings) and demands the rest again, which was Ten shillings. So that by this reaching trick, he would have had his 5 yards of Canvas of the Draper for nothing.



D 3 QUEST.

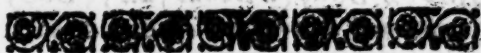
QUEST. 25.

There are 100 Stones which lie 3 foot or one yard upon the ground one from the other; and there is one employed to gather up these Stones one by one, and bring them to a Basket which standeth 3 foot from the first Stone. How many Yards of ground must he go backwards and forwards in all, before he hath brought the last Stone to the Basket?

THe number of Stones being 100, and the Basket standing one yard forward of the first Stone, makes in all 100 yards in

Recreations. 67

in length: wherefore to effect this,——Add 1 to the number of yards, it makes 101, which multiply by half the number of yards, which are 50, the product will be 5050: which shews that he must go forward 5050 yards; then must he go backwards as much, which is Ten thousand one hundred yards; which is 5 miles and three quarters, wanting only 20 yards.



D 4

QUEST.

 QUEST. 26.

 THE
 FISHER-MAN'S
 QUESTION.

*I caught a Fish (others among)
 Whose Head was full 5 foot long,
 And his Tayle was (truly)
 As long as his Head, and half his
 And his Body (without fail) (Body
 was just as long as his head & tail.*

*This is my Question,
 resolve it who can;
 How long was the Body,
 And Fishes Tail than?*

Multiply the length of the
 Fishes Head by 3, by 4,
 and

Recreations. 69

and by 8 ; the one produ& shall be the length of the Tail, the other the length of the Body ; and the third, shall be the length of the whole Fish.

So the Head being 5 foot, this multiplyed by 3, giveth 15 foot for the length of the Tail.

Again, Multiply 5 by 4, it produceth 20, for the length of the Body.

And lastly, Multiply 5 by 8, it produceth 40, for the length of the whole Fish ; and exactly answers the *Question* in all its particulars.

For the Head being 5 foot, and the Tail 15 foot, and the Body 20 foot ;

The Tail 15 foot, is equal to the whole Head 5 foot, and half the Body 10 foot : For 5 and 10 is 15.

And the Body 20 foot, is equal to 15 foot the Tail, and 5 foot the Head.

D 5

And

70 *Arithmetical*

And these together make 40 foot, the length of the whole Fish.

QUEST. 27.

There is a Steeple, the top whereof casteth its shadow upon the ground 260 foot from the bottom thereof: At the same time as you measure the shadow, the length of the shadow of your Two-foot Rule is 3 foot: I demand how high this Steeple is?

THIS Question is easily answered by the Rule of Three: but I here insert it with some others, to shew how serviceable Numbers, and the right under-

Recreations. 71

understanding of them, are applicable to all sorts of men and things. To effect this, this is the proportion :

As the length of the shadow of your Rule 3 foot, is to the length thereof 2 foot :

So is the length of the shadow of the Steeple 260 foot, to the height of the Steeple $86\frac{2}{3}$.

Wherefore, multiply 260 foot, the length of the shadow of the Steeple, by 2 foot, the length of your Rule, and the product is 520 foot ; which divide by 3, the length of the shadow of your Rule, and the quotient will be $86\frac{2}{3}$, that is, 86 foot, and two third parts of a foot, which is 8 inches ; so that the Steeple is 86 foot, and 8 inches high.

QUEST.

QUEST. 28.

There is a Fountain which hath 4 Streams; in the Cistern whereof there is contained 3 Barrels of water: if the least of the streams be only opened, the water will be 6 hours in running out: if the second, it will be 4 hours running out: If the third be opened, it will be 3 hours running out: and if the fourth and greatest be set running, it will run the water out in 2 hours. I would know in what time all the water would run out if all the 4 streams were set running together?

BEcause the least Stream will vent all the water in 6 hours,
it

Recreations.

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it must therefore vent 8 Barrels in 6 hours ; and the Second Stream would run 12 Barrels, the Third 16 Barrels, and the biggest 24 Barrels.

Least Stream—————8

Second —————12

Third —————16

Biggest —————24

—————
In all ———60

Then say by the Rule of Three,

If 60 require 6, what will 8 require ?

Multiply 6 by 8, it produceth 48, which should be divided by 60; but it being above 48, it is therefore $\frac{48}{60}$, or $\frac{4}{5}$ of an hour.

And in that time will all the water run out of the Fountain, if all the 4 Streams were set running together.

QUEST.

QUEST. 29.

A man dying, leaves his Wife with Child of her first; and by Will bequeathed his Estate, which amounted to 2600 l. conditionally thus, That if the Child his Wife went withal were a Woman-kind, that then his Wife should have two Thirds thereof, and the Child the other Third: But if she should be delivered of a man-child, then the Child was to have two Thirds, and his Wife the other Third. But after the Decease of the Father, the Mother was delivered of two Sons and a Daughter. In what nature shall this Estate be parted amongst them, according to the Testators Will?

IT is evident, by the Will of the Deceased, that for every Third that

that the Daughter was to have,
the Mother was to have two
Thirds : And that the Son was
to have double to the Mother.

Observing this Order ; if you
allow to the Daughter 1 *l.* then
the Mother must have 2 *l.* and
either of the Sons must have twice
as much as the Mother, that is
4 *l.* apiece. Wherefore for the
two Sons put down 4 *l.* and 4 *l.* ;
for the Mother 2 *l.* and for the
Daughter 1 *l.* in this order :

		1.
The two Sons	{	4
		4.
The Mother	—	2
The Daughter	—	1
		—
The Sum	—	11

Then

76 *Arithmetical*

Then say by the Rule of
Three direct,

If 11 *l.* the Sum of all the portions, requires 2600 *l.* what shall 4 *l.* (which is one of the Sons shares) require?

Multiply 2600 by 4; the product will be 10400, which divided by 11, the quotient will be 945 $\frac{5}{11}$; for one of the Sons shares: So then the other Son must have as much; and the Mother half as much; namely, 472 $\frac{8}{11}$; and the Daughter must have half as much as the Mother, namely, 236 $\frac{4}{11}$; all which being added together, make 2600 *l.* equal to the whole Estate; and answers the Will of the Testator in all particulars.

The

The two Sons $\left\{ \begin{array}{l} 945 \frac{5}{11} \\ 945 \frac{5}{11} \end{array} \right.$

The Mother ———— $472 \frac{8}{11}$

The Daughter ———— $236 \frac{4}{11}$

————— $2600 \frac{32}{11}$



QUEST.

QUEST. 30.

The Grand-father, the Father, and the Son met together, and spent 20 s. When the Reckoning came to be paid, the Grand-father would pay one Half, the Father one Third, and the Son one Quarter. How much must every one pay of this Reckoning?

TO resolve this, If the Grand-father should pay $\frac{1}{2}$, which is 10 s. and the Father $\frac{1}{3}$, which is 6 s. 8 d. and the Son $\frac{1}{4}$, which is 5 s. the Reckoning would be over-paid: for these three added together, make 21 s. 8 d. and they should pay but 20 s.

Where-

Recreations. 79

Wherefore you must work otherwise; as thus, Reduce $\frac{1}{2}, \frac{1}{3}, \frac{1}{4}$ into one denomination, by multiplying the denominators one into another; saying, 2 times 3 is 6, and 4 times 6 is 24, which 24 is a new denominator. Then the $\frac{1}{2}$ of 24 is 12: and $\frac{1}{3}$ of 24 is 8: and $\frac{1}{4}$ of 24 is 6; the sum of them is 26, — And this 26 is your first number in the Rule of Three: — 20 s. (which they spend) must be the second number; — And 12, 8, and 6 must be the three third Numbers: — Wherefore say,

I. If 26 pay 20 s. what must 12 pay?

Multiply 20 by 12, it produceth 240; this divided by 26, giveth in the quotient 9 s. $\frac{6}{26}$ for the Grand-fathers part.

II. If

80 *Arithmetical*

II. If 26 pay 20 s. what must 8 pay ?

Multiply 20 by 8, the product is 160; which divide by 26, and the quotient will be 6 s. $\frac{4}{13}$: And so much must the Father pay.

III. If 26 pay 20 s. what must 6 pay ?

Multiply 20 by 6, it giveth 120; which divided by 26, gives in the quotient 4 s. $\frac{16}{13}$: And so much must the Son pay.

The Grand-father must pay 9 $\frac{4}{13}$

	s.	d.	q.
Equal to	— 9	2	$\frac{3}{13}$

The Father must pay — 6 $\frac{4}{13}$

Equal to	— 6	1	3
----------	-----	---	---

The Son must pay — 4 $\frac{16}{13}$

Equal to	— 4	7	2
----------	-----	---	---

In all	— 20	0	0
--------	------	---	---

QUEST.

QUEST. 31.

There are Four Cities or Towns lying one from the other in a right Line; and the two farthermost are distant one from the other 56 miles: And the distance from the Third to the Fourth, is as much as from the First to the Second, with half as much as between the Second and the Third: And the distance between the Second and Third is as much as the distance between the First and Second, with the Third and Fourth together. How far were each of the Towns distant one from the other?

Let the Four Cities or Towns be A B C D.

7 B 28 C 21 D
 ———— 2 ————— 3 ————— 4

Because

82 *Arithmetical*

Because the distance between the Third and Fourth, with the distance between the First & Second, is equal to the distance between the Second and Third. Therefore divide 56 (the whole distance) by 8, and the quotient will be 7; wherefore the distance between the First and Second Town is 7 miles.

Again, it is evident, that the distance between the Third and Fourth must be three times as far, that is 21 miles. And the distance between the Second and Third being equal to both these, must be 28 miles.

So is CD distant as far as A and half BC.

And BC is distant as far as A and CD together.

And AD is distant 56 miles.

QUEST

QUEST. 32.

Two Ships set sail at one time; the one sails directly East, 74 Leagues: The other sails directly North, 62 Leagues: I would know how many Leagues these two Ships are asunder?

Multiply 74 by 74, | 5476
the product will be

Also Multiply 62 by 62, | 3844
the Product is

These two Numbers added together, make— | 9320

Of this Number 9320, extract the square Root, and you shall find it to be almost 97: And so many Leagues are the two Ships asunder

QUEST.

QUEST. 33.

There was a May-pole, which in a windy night was broken, so that the top thereof lit upon the ground 30 foot distant from the bottom thereof; and the piece which was broken off was 50 foot long: At what length was the May-pole broken off, and how high was it in all?

Multiply 50 (the length of the piece broken off) by itself; that is, Multiply 50 by 50, it makes 2500. Likewise multiply 30 (the distance which it fell from the bottom) by 30 the Product is 900; Subtract

Recreations. 85

900 from 2500, and there remains 1600: Extra^d the square Root of 1600, and you will find it to be 40; so that there is 40 foot of the May-pole standing: and 50 being broken off, makes 90; so that the May-pole was 90 foot high.

30
bot-
iecc
wa
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pol
big

th
) i
o b
ewi
whic
y 30
ttrac
90

E QUEST.

QUEST. 34.

There is 160l. to be distributed amongst a number of poor People; some are to have shillings, some six-pences, some Groats, and some Threc-pences: How many poor People will this relieve, so that the number of those that receive shillings, six-pences, groats, and three-pences, shall be equal?

TO effect this, reduce the 160l. into pence; it maketh 38400 pence for your dividend. Then add 12 d. 6 d. 4 d. and 3 d. together, they make 25 d. and this is your Divisor.

Then

Recreations. 87

Then divide 38400 (the pence in 160 l.) by 25 (the sum of the shares) and in the quotient you shall find 1536; and so many poor people must there be of a sort: which you may easily thus prove: For,

		l.	s.	d.
1536	{ Shillings—	{ is	76	16-0
	{ Six-pences—		38	08-0
	{ Groats—		25	12-0
	{ three-pences		19	04-0

In all—160-00-0

Now if you would know how many Poor there were in all, Multiply 1536 by 4, and the quotient will be 6144; and so many poor People must there be in all, to receive this Legacy.

E 2 QUEST.

QUEST. 33.

There was a May-pole, which in a windy night was broken, so that the top thereof lit upon the ground 30 foot distant from the bottom thereof; and the piece which was broken off was 50 foot long: At what length was the May-pole broken off, and how high was it in all?

Multiply 50 (the length of the piece broken off) in it self; that is, Multiply 50 by 50, it makes 2500. Likewise multiply 30 (the distance which it fell from the bottom) by 30 the Product is 900; Substrac

Recreations.

85

900 from 2500, and there remains 1600: Extract the square Root of 1600, and you will find it to be 40; so that there is 40 foot of the May-pole standing: and 50 being broken off, makes 90; so that the May-pole was 90 foot high.



E QUEST.

QUEST. 34.

There is 160*l.* to be distributed amongst a number of poor People; some are to have shillings, some six-pences, some Groats, and some Threc-pences: How many poor People will this relieve, so that the number of those that receive shillings, six-pences, groats, and three-pences, shall be equal?

TO effect this, reduce the 160*l.* into pence; it maketh 38400 pence for your dividend. Then add 12 *d.* 6 *d.* 4 *d.* and 3 *d.* together, they make 25 *d.* and this is your Divisor.

Then

Recreations. 87

Then divide 38400 (the pence in 160 l.) by 25 (the sum of the shares) and in the quotient you shall find 1536; and so many poor people must there be of a sort: which you may easily thus prove: For,

			l. s. d.	
1536	{	Shillings—	} is {	76-16-0
		Six-pences—		38-08-0
		Groats—		25-12-0
		three-pences		19-04-0

In all——160-00-0.

Now if you would know how many Poor there were in all, Multiply 1536 by 4, and the quotient will be 6144; and so many poor People must there be in all, to receive this Legacy.

E 2

QUEST.

QUEST. 35.

How many persons will there be required to receive 2880 Pence, some receiving 6 d. some 5 d. some 4 d. some 3 d. some 2 d. and some 1 d. there being a like number of each sort?

IF you add 6d. 5d. 4d. 3d. 2d. & 1d together, they make 21 d. by which, if you divide 2880, the quotient will be $137\frac{1}{7}$; and so many persons must there be of a kind: which is thus proved:

For,

137

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pen
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288
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sum

Recreations. 89

For, l. s. d.

137	{	Six-pences—	}	is	{	3- 8--6
		Five-pences—				2-17--1
		Groats—				2- 5--8
		three-pences				1-14--3
		Two-pences				1- 2-10
		Pence—				0-11--5

In all———11-19--9

This 11*l.* --19*s.* --9*d.* should have been 12*l.* equal to 2880 pence; but by the former work you see that when you divide 2880 by 21, there remained $\frac{7}{21}$, or $\frac{1}{3}$ (which is all one) now this $\frac{1}{3}$ becomes to be $\frac{21}{7}$ of a penny, which is equal to 3*d.* wherefore if you add 3*d.* to 11*l.* --19*s.* --9*d.* the sum will then be 12*l.* or 2880*d.*

E 3

QUEST.

QUEST. 36.

There are 1000 Loaves of Bread to be divided amongst 3 sorts of Persons, those that were above 40 years of age, were to have 12 penny loaves, those above 20 years of age were to have 6 penny loaves, & those above 10 years of age were to have penny loaves. How many 12 penny loaves, how many 6 penny, and how many penny loaves must there be provided?

The excess is $\begin{Bmatrix} 40 \\ 20 \\ 10 \end{Bmatrix}$ for the $\begin{Bmatrix} 1 \\ 2 \\ 3 \end{Bmatrix}$ sort of persons

The sum—70

By

Recreations. 91

By the Rule of Three say,

(1) If 70 require 1000, what shall 40?

Multiply 1000 by 40, it produceth 40000; which divide by 70, the quotient will be $571\frac{3}{7}$, and so many 12 penny loaves must be provided.

(2) If 70 require 1000, what shall 20?

Multiply 1000 by 20, it produceth 40000; that divided by 70 produceth $285\frac{5}{7}$, so many 6 penny loaves.

(3) If 70 require 1000, what shall 10?

Multiply 1000 by 10, it produceth 10000; this divided by 70 produceth $142\frac{6}{7}$, and so many penny loaves must be provided: which added together, (the fraction-parts excepted) make 1000 loaves.

E 4 QUEST.

QUEST. 37.

A Debtor owes his Creditor a certain sum of money, of which, because he cannot make one entire payment, condescends to pay it by the weeks in the year, according to this progression, namely, to pay the first week 5s. the second week 10s. the third week 15s. &c. I would know how much the Creditor received of his Debtor at the years end?

TO perform this easily (for to add 5s. 10s. 15s. 20s. till you come to the end of the 52 weeks,

Recreations. 93

weeks, which make a year, would be tedious) do thus;

First multiply 52 (the number of weeks in the year) by 5 (the increase every week) 260, which is equal to the two and fiftieth number, if you had added the sums together.

Secondly, to this 260, add 5 (the increase for one week) it maketh 265, which multiply by 26 (half the number of weeks in the year) and it produceth 6890 shillings, which is 344^l. 10s. and so much will the Creditor have received of his Debtor at the years end.

E 5 QUEST:

QUEST. 38.

A certain person by Will, bequeaths his Estate to his Executor, enjoying him every year (so long as the Executor lived) to bestow on certain charitable uses by him named, a certain sum of Money, increasing every year 55 l. more than the preceding; so the first year the Executor expended 55 l. and the last year 495 l. How many years lived the Executor after the Donor? and how much to the fore-mentioned Uses did he expend?

TO effect this easily, First, Subtract 55 l. (the first disbursement) from 495 l. (the last disbursement) the remainder is 440 l. which divide by 55 (the Excess

Excess or increase of every years disbursement) and the quotient will be 8, to which add 1, and it makes 9; and so many years lived the Executor after the Deceased.

Secondly, Multiply 55 (the Excess) by 9 (the number of years) the quotient will be 495, which was the last disbursement.

Thirdly, add 495 and 55 together, they make 550, which multiply by $4\frac{1}{2}$ (which is half the number of years the Executor lived) and the product will be 2475; and so much did the Executor expend in all.

QUEST.

QUEST. 39.

A Father gave to his eldest Son 252 l. and to his youngest he gave but 28 l. and to every son successively from the youngest he gave 28 l. more than to the other. How many sons had the Father? and how much Money did all their Legacies amount unto?

First take 28 (the youngest Sons share) from 252 (the eldest Sons share) the remainder will be 224. which divide also by 28 (because every Sons portion exceeded others by 28 l.) and the quotient will be 8, to which add 1 (for the first Son) and it makes

Recreations: 97

makes 9; so that he had 9 Sons.

Now to find what sum of Money all their Legacies amounted unto; add 28 (the youngest Sons share) to 252 (the eldest Sons share) and the sum will be 280; which being divided by $4\frac{1}{2}$ (which is half the number of the Sons he had) the Product will be 260*l*. and so much Money did all their Portions amount unto.



QUEST.

QUEST. 40.

A Bishop dying, left 10000 l. to be distributed amongst three sorts of Men, viz. Divines, Lawyers, and Physicians, in such order, that 40 Divines were to have 10 l. the Lawyers 5 l. the Physicians 1 l. And 60 Physicians were to have their parts out of the Legacy also. I would know what the Divines, Lawyers, and Physicians share will be? And also what will the Portion or share of every Divine, Lawyer and Physician be?

First Multiply 40 (the Divines) by their Excess (which is

Recreations. 99

is 10 l.) and it produceth 400.

Secondly, Multiply the 50 Lawyers by 5 (which is their excess) and it produceth 250.

Thirdly, Add these two numbers together, viz. 400, and 250, and they make 650, which with the 60 Physicians make 710, the total, as here you see;

Divines ——— 400

Lawyers ——— 250

Physicians ——— 60

In all ——— 710

Being thus prepared, say by the Rule of Three direct thus;

If 710 persons have 10000 l. amongst them, how much shall 400 persons have?

First, for the Divines.

Multiply 10000 by 400, it produceth 4000000; which divide by 710, and the quotient will be

100 *Arithmetical*

be 5633 l. and $\frac{57}{71}$ of a pound; so that the 140 Divines shares will come to 5633 $\frac{57}{71}$ l.

Secondly, for the Lawyers.

Multiply 10000 by 250, the Product will be 2500000, which divide by 710, and the quotient will be 3521 l. and $\frac{9}{71}$ of a pound; so that the 250 Lawyers will have 3521 $\frac{9}{71}$ l. for their shares.

Thirdly, for the Physicians.

Multiply 10000 by 60, the product will be 600000, which divide by 710, and the quotient will be 845 and $\frac{5}{71}$ of a pound. So that the 60 Physicians will have for their shares 845 $\frac{5}{71}$ l. All which shares being added together, do make up the just sum of 10000 l. As here you see.

400 Divines	—	5633 $\frac{57}{71}$
250 Lawyers	—	3521 $\frac{9}{71}$
60 Physicians	—	845 $\frac{5}{71}$

10000

Having

Recreations. 101

Having thus found the general shares, it will be now requisite to find every Particular share: and

First, for every Divines share, say,

If 40 Divines have 5633 $\frac{57}{71}$ l. what shall one have?

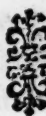
Divide 5633 $\frac{57}{71}$ l. which is 5633 l. -- 16 s. -- 0 -- 2 q. $\frac{50}{71}$. by 40, the quotient will be 140 l. -- 16 s. -- 0 d. -- 3 q. $\frac{19}{71}$. for every Divines share.

Secondly, for every Lawyers share.

Divide 3521 $\frac{2}{71}$, which is 3521 l. -- 2 s. -- 6 d. -- 1 q. $\frac{49}{71}$, by 50, the quotient will be 70 l. -- 8 s. -- 5 d. -- 1 q. $\frac{46}{71}$. for every Lawyers share.

Thirdly, for every Physicians share.

Divide 845 $\frac{5}{71}$, which is 845 l. -- 1 s. -- 4 d. -- 3 q. $\frac{43}{71}$, by 60, the quotient will be 14 l. -- 1 s. -- 8 d. -- 1 q. $\frac{2}{71}$, for every Physicians share.



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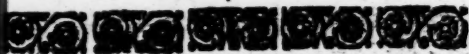
A
SUPPLEMENT
to the foregoing
QUESTIONS.

THe foregoing 40 Questions *not of themselves* being sufficient to make a Treatise answerable, in bulk, to the Stationers desire; I have therefore, for his satisfaction, added the particulars following, (being no less useful then profitable, and altogether as Recreative and delightful, as the former)
namely,

namely, Ten Questions, put pro
by way of Proposition, with mo
the Answers of them, which Num
will give sufficient light to and
the Practitioner, to resolve ther
and confirm him in the reall,
solving of the like, when Con
they shall be proposed to tick
him. ----- After these Propo- use.
sitions, I have added (by way Ari
of Discourse) several A-
greements and Contracts be-
tween party & party, seem-
ing fair and reasonable at
the proposing, which the sub-
tilty of Numbers discovers
to be either impossible in the
performance, or fallacious in
the intent of the party that
offers them. ----- Likewise, I
have declared the subtilty,
propriety,

propriety, and secret harmony that there is in some Numbers, both in themselves, and being joyned with others. ----- And to conclude all, I have added diverse Compendiums in Arithmetick, which will be of good use, and ease you in many Arithmetical performances.

Vale.



APPEN-

*Appendix.*

TO the foregoing *Questions*, I will here add certain *Propositions*, and give the *Answers* of them in general terms, leaving the *Arithmetical Working* of them to the ingenious *Practitioner*, thereby the better to confirm him in his undertakings, to resolve other *Questions* that may be proposed to him.

P R O

PROPOSIT. I.

There were 6 Cups of Gold which weighed together 600 ounces, but each Cup was heavier than the other by one ounce; now how much did each Cup weigh severally?

Ans. One (and the least of the Cups) weighed 99 ounces and a half; the next 100 and a half, the third 101 and a half, the fourth 102 and a half, the fifth 103 and a half, and the sixth and biggest weighed 104 ounces and a half; all which numbers being put together, make 600 ounces, equal to the whole weight.

PROP.

PROP. II.

There are Four several Measures, as A. B. C. D. of which D holds 24 pints, and C holds as much again as B, and 3 times as much as A; and D with twice A, will hold double as much as C, and four times as much as B. How much did every one of these Measures hold severally?

A *Answer.* A holds 6 pints,
 D 24
 C 18
 B 9

So that C holds as much again as B, and three times as much as A, and D with twice A, holds as much as C, and four times as much as B.

PROP.

PROP. III.

A Father leaves 1000 l. to be disposed of to his Son and Daughter, conditionally thus; That the fifth part of that which his Son should have, should exceed the fourth part of that which the Daughter should have, by 10 l. What must each have?

Ans^r. **T**He Son had 577 l. and $\frac{7}{9}$ of a pound; and the Daughter 422 l. and $\frac{2}{9}$ of a pound. Now the fifth part of 577 $\frac{7}{9}$ is 115 $\frac{5}{9}$; — And the fourth part of 422 $\frac{2}{9}$ is 105 $\frac{5}{9}$, which is less then 115 $\frac{5}{9}$ by 10: — And 577 $\frac{7}{9}$ and 422 $\frac{2}{9}$ being added together, do make 1000 l. equal to the whole Legacy.

PROP. IV.

One coming into an Orchard, asked the Gardner how many Trees there were in that Orchard? The Gardner answered, That the one half of the trees were Apple-trees, the Quarter-part Pear-trees, the seventh-part were Plumb-trees, & that there were 12 Cherry-trees besides. How many trees were there in this Orchard?

Ans. **T**Here were 112, the half whereof is 56, the quarter thereof is 28, and the seventh part is 16; these three numbers added together, make 100, which with the 12 Cherry-trees make in all 112 Trees in the Orchard.

PROP.

Answ

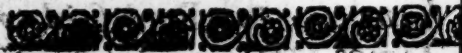
PROP. V.

Two Persons, as James and Paul, had between them a certain number of Sheep in two Drovers; James said to Paul, If you put 70 of your Sheep into my drove, I shall have three times as many Sheep as you have: --- But Paul said to James, If you put 70 of yours into my drove, I shall have five times as many as you. How many Sheep had each of them?

Ans. James had 110, and Paul had 130, — For if you
 F 2 take

112 *Arithmetical*

take 70 from *Paul* and add them to *James*, then *James* will have 180, and *Paul* but 60, which is but one third part of what *James* hath : — But if you take 70 from *James* and give them to *Paul*, then *Paul* will have 200 and *James* but 40, which is but one fifth part of what *Paul* hath.



PRO

PROP. VI.

The Father and Son travelling together, each of them carrying a certain number of Bottles of Wine; the Son complains to the Father, that he was overladen: the Father replied, If I should take one of your Bottles, then I should have as many more Bottles as you have; and if I should give you one of mine, yet I should have as many as you have in all still. How many Bottles had each of them?

Ans. **T**He Father had 7, and the Son had 5. — So if

114 . *Arithmetical*

if the Father had taken one of the Sons Bottles from him, the Son would have had but 4, and the Father 8, which is double the Sons number; and if the Son had taken one from the Father, then they would have been both equal, for either of them would have had 6 Bottles.—Many other numbers may be found to do the like, which I leave for you to discover.



P R O P.

Ans

PROP. VII.

One having in the Market a Basket of Apples, another comes and asks him how many there is of them? the Owner replies, He cannot tell; but he remembers, that when he told them into his Basket by two and two, there was one odd one at last: Also when he told them in by three & three, there was still one odd one; and also by four and four, there was still an odd one remaining; the like when he told them in by five and five, and by six and six, still one odd one remained: but when he told them in by seven and seven, then they fell even. How many Apples were there in his Basket?

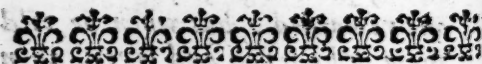
Ans. **H**E had 721, which number being divided by

F. 4

2, or

2, or 3, or 4, or 5, or 6, there will still remain 1; but being divided by 7, there will remain nothing.

For 2, 3, 4, 5, 6, being multiplied continually into themselves, will at length produce the number 720, to which add a unite, and it is 721, the number sought. — There are many other numbers which will afford the like, which I leave to your practice to find of your self.



P. R. O. P.

PROP. VIII.

If one should buy 12 loaves of bread for 12 pence, so that some of them may be two penny loaves, some penny loaves, some half-penny loaves, and some farthing loaves; How many of a sort must he buy?

Ans^r **H**E must buy 3 two-penny loaves, 4 penny loaves, 3 half-penny loaves, and 2 farthing loaves.

For,	d.
3 two-penny loaves are—	6
4 penny loaves are—	4
3 half-penny loaves are—	$1\frac{1}{2}$
2 farthing loaves are—	$0\frac{1}{2}$

12 Loaves.	—————	Pence—12
	F 5	There

118 *Arithmetical*

There are other numbers will do the same; which I leave to your finding out.

PROP. IX.

There is 1000 l. to be distributed amongst 10 persons, namely, some Men, some Women, some Male-children, and some Female-children; with this condition, That every Man must have 50 l. every Woman 70 l. every Male-child 130 l. and every Female-child 150 l. How many must there be of each sort?

Ans. **T**here may be 2 Men, 3 Women, 3 Male-children, and 2 Female-children.

For

Recreations. 119

For, l.

2 Men, at 50 l. a piece must have 100

3 Women at 70 l. must have 210

3 Male-ch. at 130 l. must have 390

2 Fem. ch. at 150 l. must have 300

10 Persons Pounds—1000

There are other numbers will do the like, which I leave for your practice to find out.



PROP.

PROP. X.

A Man dying, and leaving seven Sons, bequeaths his Estate in Money to be thus divided; One half to his eldest son, the half of the remainder to his second son, the half of the remainder to his third son, and so to all the seven; and the remaining half to an Executor to see his Will performed; which remaining half was 34l. What was his whole Estate? and what every Childs part?

Answ. **H**is whole Estate was 8670l. And of this, the

Recreations.

121

the Executor had	1.
The seventh Son had	34
The sixth Son	68
The fifth	136
The fourth	272
The third	544
The second	1088
The first	2176
	4352
In all	8670



Concerning



Concerning two Neighbours Changing of their Land.

Two Neighbours had either of them a piece of Land, the one field was four-square, every side containing 120 perches, so that it was round about 480 perches. — The other was square also, but the sides longer than the others field, and the ends shorter; for the sides of this field were 140 perches long apiece, and the ends thereof were 100 perches apiece; so that this field was 480 perches about as well as the other. Now which of these two had the best bargain?

IT is wonderful to see how Numbers will discover that to be

be erroneous and absurd, which to common sense and mans apprehension appears reasonable; as in this bargain. — First, for the field which is 120 perches on either side. — Multiply 120 by 120, and the product is 14400; and so many square perches doth that piece of Land contain, that is 80 acres. — Then for the other field, — Multiply 140 (the length of one of the longer sides of the field) by 100 perches (one of the shorter sides) and the product will be 14000 perches, the content of the other field, which is less then the former by 400 perches, that is 2 Acres and an half; and so much would he have lost that had the field of 120 perches on every side, though the other field were as much about.

And this error would still grow greater, the narrower the second field

field had been: As suppose the ends or shorter sides thereof had been but 40 perches apiece, and the longer sides 200 apiece, this field would still have been 480 perches about: but let us see how much it contains. — Multiply 200 the longer side, by 40 the shorter side, and it will produce 8000; and so many square perches will it contain, which is but 50 Acres: So that if he had changed for this field, which is as much about as his, he would have then lost 30 Acres by the bargain.

About

E



About the borrowing of Corn.

A Country Farmer had in his house a vessel of Wood full of Wheat, which was 4 foot high, 4 foot broad both at top and bottom; and in all parts 4 foot, as the sides of a Die. — One of his Neighbours desires him to lend him half his Wheat till Harvest; which he doth: — Harvest coming, and his Neighbour is to repay; he makes a Vessel 2 foot every way, as his Neighbors was 4 foot every way, and fills him that twice, in lieu of what he borrowed. Was there gain or loss in this particular?

EXamine first what either of these Vessels will hold, and by

F26 *Arithmetical*

by that you will discover the fallacy. — First, the vessel 4 foot high, contains 48 inches of a side; wherefore multiply 48 by 48, and the product will be 2304, which multiply again by 48, and the product will be 110592; and so many cubical or square inches of Corn did his vessel hold; the half whereof, wch is 55296 he lent his Neighbour. Now secondly, let us examine how much the second vessel will hold, it being 2 foot on every side, that is 24 inches; — Multiply 24 by 24, the product is 576: which divide again by 24, and the product will be 13824; and so many Cubical or square inches did the lesser vessel contain; which being filled twice, it made 27648 Cubical inches of corn or wheat, which was all he paid his Neighbour in lieu of the 55296 inches which he borrowed, which is but

the

the just half; and so allowing 2256 cubical inches of Wheat to make a Bushel (for so many there is in a Bushel) he paid his Neighbour less by 12 bushels, and about a peck, than he borrowed of him. And this, and the reason of it is evident, as I will demonstrate to you by a familiar president. — If you cause a Die to be made of one inch every side, and 8 other Dies to be made of half an inch every side, these 8 being laid close one to another in a square form, these 8 will be out of the same bigness with the other one Die, whose side is but an inch.



A Bargain



A Bargain between a Farmer and a Goldsmith.

A rich Farmer being in a Fair, espies at a Goldsmiths Shop a Neck-lace of Pearl, upon which were 72 Pearls: the Farmer cheapning of it, the Goldsmith asked 30s. a Pearl; at which rate the Neck-lace would come to 103l. The Farmer looking upon it as dear, goes his way, offering nothing. Whereupon the Goldsmith calls him, and tells him, if he thought much to part with Money, he would deal with him for Corn: — To which the Farmer hearkens; asks him how much Corn he would have for it at two shillings the Bushel: The Goldsmith

Goldsmith told him he would be very reasonable, and would take for the first Pearle one Barly corn only, for the second two corns, for the third four corns; and so doubling the corns till the 72 Pearls were out. To this the Farmer agrees; and immediately strikes the Bargain: But see the event.

HE that hath any skill in Numbers, will easily discern the vanity that there is in this kind of bargaining; so that no man can be bound to them: for Numbers increasing in a Geometrical Progression, do so prodigiously increase, that (to those that are ignorant of the reason) it will seem impossible they should do so; but that it is so, will appear evident by this bargain, if you enquire, First, The quantity: Secondly, The worth of so much



A Bargain between a Farmer
and a Goldsmith.

A rich Farmer being in a Fair, espies at a Goldsmiths Shop a Neck-lace of Pearl, upon which were 72 Pearls: the Farmer cheapning of it, the Goldsmith asked 30 s. a Pearl; at which rate the Neck-lace would come to 103 l. The Farmer looking upon it as dear, goes his way, offering nothing. Whereupon the Goldsmith calls him, and tells him, if he thought much to part with Money, he would deal with him for Corn: — To which the Farmer hearkens; asks him how much Corn he would have for it at two shillings the Bushel: The Goldsmith

Goldsmith told him he would be very reasonable, and would take for the first Pearle one Barly corn only, for the second two corns, for the third four corns; and so doubling the corns till the 72 Pearls were out. To this the Farmer agrees; and immediately strikes the Bargain: But see the event.

HE that hath any skill in Numbers, will easily discern the vanity that there is in this kind of bargaining; so that no man can be bound to them: for Numbers increasing in a Geometrical Progression, do so prodigiously increase, that (to those that are ignorant of the reason) it will seem impossible they should do so; but that it is so, will appear evident by this bargain, if you enquire, First, The quantity: Secondly, The worth of so much

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much Barley in Money : and,
Thirdly, the weight of it, and
how it should be removed, or
where stowed. Wherefore,

1. If we allow 10000 *ten thousand* corns to a Pint, (which is more then enough) then 5120000 corns will make a Quarter; but yet (for the ease of them that will make tryal) we will allow 10000000 corns to make a Quarter; by which number, if you divide the whole number of corns that the 72 Pearls would have amounted unto, being doubled, (which by cutting off the 7 last figures towards the right hand) the Quotient of that Division would be

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and so many whole Quarters of Barly would the Neck-lace have amounted unto, and some odd Bushels, which we here omit as superfluous.

2. Now

Recreations. 131

2. Now for the worth of this Barly, suppose it were sold at 15d. the Bushel, (which is a reasonable rate) that is 10 s. the Quarter: wherefore divide the foregoing number of Quarters by 2, that is, take half of it, and it will be 236118324143482 pounds sterling; which sum rendered in words, is, *Two hundred thirty six millions of millions, one hundred and eighteen thousand, three hundred twenty four millions, one hundred forty three thousand, four hundred eighty two pounds.* A vast sum of money for a Farmer. And thus, if you reckon Land forever worth 20 years purchase, if you divide this sum of pounds by 20, the Quotient being 11805916202174, is the yearly Rent thereof: which is, *Eleven millions of millions, eight hundred and five thousand nine hundred and sixteen millions, two hundred and two*

132 *Arithmetical*

two thousand, one hundred seventy four pounds a year. And again, if you divide this number of pounds by 365 (the number of dayes in a year) the Quotient will be 32344975918 ; that is, Thirty two thousand, three hundred forty four millions, nine hundred seventy five thousand, nine hundred and eighteen pounds a day for ever. So great vanity may be agreed and concluded upon by people ignorant of this Science, and for want of serious premeditation. But

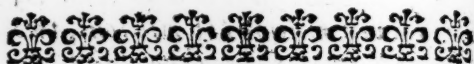
3. Let us consider the weight of so much Barley. If we allow 8 Bushels (or one Quarter) to weigh Two hundred weight (but doubtless it weighs more) then the whole number of Quarters multiplied by 2, gives the weight of all the Barley to be 944473296573928 hund. weight. And if you divide this number

Recreations. 133

by 20, the Quotient will be 47223664828696 Tuns; that is, Forty seven millions of millions, two hundred twenty three thousand six hundred sixty four millions, eight hundred twenty eight thousand, six hundred ninety six Tuns; which will require 47223664828; that is, Forty seven thousand two hundred twenty three millions, six hundred sixty four thousand, eight hundred twenty eight Ships of a thousand Tun apiece to carry it. And to conclude, If there were four Millions of Nations in the World, and every one of those Nations had Ten thousand Sail of such Ships of a Thousand Tun apiece; yet all those Ships would not contain it. Thus by this you may see, how prodigiously numbers do increase, being multiplied according to Geometrical Progression.

G

Con-



Concerning an Agreement
that a Country-Fellow
made with a Farmer.

A Country-Fellow comes to a Farmer, and offers to serve him for 8 years; all which time he would require no other Wages than One grain of Corn, and one-quarter of an inch of Land to sow it in the first year; and Land enough to sow that one Corn, and the increase of it, for his whole 8 years: to which the Farmer assents.

THeir Bargain being thus made, let us consider what his eight years service will be worth.

Recreations. 135

worth. For the first year he hath only one quarter of an inch of Ground, and one Corn; which Corn we will suppose had in the Ear at the years end 40 Corns, (for that is few enough:) then the second year he must have 40 square quarters of inches of ground to sow those 40 Corns in, that is, 10 square inches of Ground. And the third year, supposing those 40 Corns to produce 40 Ears, and in each Ear 40 Corns, as before, they will be in the third year increased to 1600 corns; so that he must have 1600 square quarters of inches to sow that increase in, which is 40 square inches; and thus continuing till the 8 years be expired, the increase would be 655360000000000 corns; that is, Six millions of millions, five hundred fifty three thousand and six hundred millions of corns; and so

G 2

many

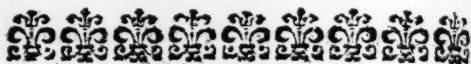
136 Arithmetical

many square quarters of inches of Land must he have to sow this increase in. Now know that 36000000000 corns, that is, *Three thousand and six hundred millions of square inches*, do make a mile, upon the superficies of a plain; and that superficies of a Mile will be capable to receive 144000000000; that is, *Fourteen thousand and four hundred millions of Corns*: wherefore divide—
 65536000000000 (the whole number of the Corns increase) by 144000000000, (the number of Corns that one Mile square of Land is capable to receive) and in the Quotient you shall have 455; and so many miles square of Land must there be, to contain the sowing of the increase of one Corn in 8 years, which will be about 420000; that is, *Four hundred and twenty thousand Acres of Land*; which being rate

Recreations. 137

rated at half a Crown an Acre
by the year, it will amount unto
50000; that is, *Fifty thousand*
pound; which is 6250, that is,
Six thousand two hundred and fifty
pound a year: a very considerable
Salary for Eight years service.

By these, and the like Con-
tracts, we may see what ab-
surdities are and may easily
be committed, which you
see the subtilty of Numbers
easily discovers. I will give
you by way of Discourse,
some presidents concerning
the increase of Creatures
of several kinds, which you
may make tryal of for your
Recreation; As,



I.

WHat think you, if one should tell the Great Turk (or any other Potentate in the World, who having a great Army in the Field in continual pay) that all the Revenue appertaining to his Crown, will not for one years time maintain all the Pigs that one Sow, with all the Pigs of her race, and the increase issuing of them, shall produce in 12 years; notwithstanding he can maintain so great an Army in the field. Doubtless, he would take it unkindly: But consider; Imagine the Sow brings forth but 6 Pigs at a Litter; of which we will allow 2 to be Barrow, (and this supposition is as little

Recreations. 139

as may be) and then imagine that every of those 4 bring as many every year, and the increase of them the like, during the term of 12 years; they and their race at the end of the time will be increased to *Three and thirty millions* of Pigs: Now if we allow 5 shillings for to maintain one of these Pigs for a year, which is not full half a farthing a day; yet there must be *Three and thirty millions* of Crowns to maintain them one year: which will make a great hole in a large Revenue.



G 4. Would



I I.

Would any man (that hath not skill in Numbers) imagine that 100 Sheep, and the increase thereof being preserved for the space of 16 years, should be worth above *One million, six hundred and twenty thousand pound sterling*? Yet if every Sheep do produce but one every year, at the expiration of 16 years, 100 sheep will increase unto 6553600; which is, *Six millions, five hundred fifty three thousand, six hundred Sheep*: now supposing these to be worth but 5 shillings apiece, they would at that rate amount unto 1638400; that is, *One million, six hundred thirty eight thousand four hundred pounds sterling*.



III.

IN Numbers there is a subtile property, which some have above others; of which I will give you a few : As,

1. Is it not strange that there is but one whole Number to be found, which being doubled, shall produce the same sum as it would if it were multiplied in it self squarewise? and that is the number 2 : for 2 and 2 added together, make 4 ; and so if you multiply 2 by 2, it shall produce 4 also : and you can find no other whole number which hath the like property.

2. There is a secret property in the numbers 5 and 6 ; for if you multiply either of these

G 5

num-

142 *Arithmetical*

numbers in themselves, the numbers produced by those multiplications, shall terminate or end in themselves: as 5 multiplied by 5, produceth 25, which also ends in 5. Likewise 6 multiplied by 6, produceth 36, which terminates in 6 also. Also if any greater numbers ending in 5 or 6, be yet farther multiplied by 5 or 6, they will continually terminate or end in 5 and 6. So 325 multiplied by 5, produceth 1625; and 746 multiplied by 6, produceth 4476; the one ending in 5, the other in 6.

3. The number 9 hath a privilege above all other numbers; for if you take any number, the nines taken in the gross sum all together, or in the parts severally, will be still the same; as in the number 36, it makes 4 times 9; so that if you take the nines out of 36, they are in number 4:
and

Recreations: 143

and if you multiply 9 by 4, it will also produce 36; also if you take the nines out of 240, it is all one as if you should take the sum of the simple figures 2, 4, and 0; for 2 and 4 is 6: so if you divide 240 by 9, you shall find 6 remaining, which is equal to 4 and 2.

4. There is a fine harmony between these two numbers 220 and 284, that the aliquot-part of the one, do make up the sum of the other; as thus, The parts of 220 are 110, 55, 44, 22, 20, 11, 10, 5, 4, 2, 1: the sum of which aliquot-parts do make 284; and the aliquot-parts of 284, are 142, 71, 4, 2, 1; which added together make 220: and this harmony is not to be found in many other numbers.

5. But the number 6 hath an eminent Propriety, for his parts are equal to himself; thus his
half

half which is 3, his third which is 2, and his sixth part which is 1, being added together, do make 6; and how rare such numbers are to be found, do you judge; for between One, and ——— 1000000000000, that is, One million of millions, there are but Ten of such Numbers to be found, and those are these:

1	6
2	28
3	486
4	8128
5	120816
6	2096128
7	33550336
8	536854528
9	8589869056
10	137438691328

In which Numbers you may observe, that orderly and successively, One ends in 6, the next
in

in 8; that is, every odd number, as the first, the third, the fifth, the seventh, and the ninth, do end in 6, whose half is 3, an odd number; and the even places, as the second, fourth, sixth, eighth, and tenth numbers end in 8, the half thereof being 4, an even number. And if you proceed to find more of these Numbers, you may find the twentieth Number, that hath this quality, to be——

-151115727451553768931328.

6. In Square and Cube Numbers there are subtile properties, as, if from an Unite you do successively add the odd numbers, all those numbers shall be square numbers; as if to 1, or Unity, you add the next odd number which is 3, the sum is 4 a square number,

146 *Arithmetical*

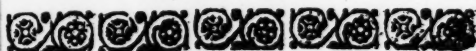
number ; to which add 5, the next odd number, and the sum is 9, a square number also; to which add 7, the next odd number, and the sum is 16, a square number also; and so on, as in this little Table.

For	1	&	3	is	4	Square Numbers.
	4		5		9	
	9		7		16	
	16		9		25	
	25		11		36	
	36		13		49	
	49		15		64	
	64		17		81	
	81		19		100	

So

So likewise, if Cubick Numbers be successively added from Unity, these Numbers shall also be Square Numbers.

7. It is worth the observing, that no exact Square Number can end with any of these figures; as 2, 3, 7, or 8.



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Compendious
RULES
IN
ARITHMETICK.

By which
Some seeming Difficulties
and common Obstacles
are removed, and the
performance of them
rendred familiar and
easie.

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Compendium I.

In the dividing of any great Sum, how you shall certainly know what Figure to put in your Quotient; so that you shall never take too much, nor too little, but alwayes the right; and divide your Sum by Substraction only, without Multiplication.

First, write down all the nine Digits orderly one under another,

152 *Arithmetical*

nother, and then by the side of them draw a right line, and against the figure 1, (towards your right hand) set down your Divisor, and multiply it by all the 9 Digits, so shall you see against every figure how much the Multiplication of your Divisor by any Digit will amount unto: So that when you see your Remainder in your Division, look in this little Table for the nearest number less then your Remainder; and that figure which standeth against that Number, you must alwayes put in your quotient.

Example.

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2
3
4
5
6
7
8
9

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Recreations. 153

Example. Suppose you were to divide any great Sum (as 98204602) by 3989,

	<i>Divisor</i>
1	3989
2	7978
3	11967
4	15956
5	19945
6	23934
7	27923
8	31912
9	35901

your first work is to ask, How many times 3989 (your divisor) can you have in 9820, the 4 first figures of your dividend. —

Look in this little Table for the nearest number you can to 9820, which is less, and you shall

find the nearest number less, to be 7978, which number standeth against the figure 2, wherefore set 2 in your quotient, and subtract 7978 out of 9820, and there will remain 1842 ; to which the next figure of your dividend being added, makes it 18424. Then you are to ask, how many times 3989 you can have in 18424.

Look

154 *Arithmetical*

Look in your Table for the nearest number to 18424, and you shall find the nearest less to be 15956, against which stands the figure 4; therefore place 4 in the quotient, and subtract 15956 out of 18424, and there will remain 2468, which with the next figure of your Dividend 6, maketh 24686.—Then ask how often you can have 3989 in 24686; the nearest number in the Table less than this, is 23934, against which stands 6: place 6 in your quotient, and subtract 23934 from 24686, and there remains 752, which with the next figure of your dividend 0, makes 7520.—Then ask how often you can have 3989 in 7520; look for the nearest number to 7520, and you shall find the nearest number less to be your divisor, 3989, standing against the figure 1; wherefore place 1 in the quotient, and subtract

Recreations. 155

subſtraſt 3989 out of 7520, and there will remain 3531, which with the next figure of your dividend 2, maketh 35312. — Then ask how many times 3989 can you have in 35312; the neareſt number in the Table leſs, is 31912, againſt which ſtands the figure 8: ſet 8 in your quotient, and ſubſtraſt 31912 from 35312, and there will remain 3400. — And ſo is your diviſion ended, the quotient being 24618, and ³⁴⁰⁰3989 remaining.

I hvae

156 Arithmetical

I have here inserted this Example, though not after the usual way of Division; but it may be used to any kind as well as this.

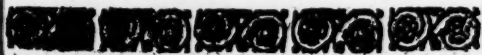
$$\begin{array}{r}
 \text{Remai.} \\
 (3400 \\
 3531 \\
 752 \\
 2468 \\
 1842 \\
 \text{Divis. } 3989 \) \ 98204602 \ (24618 \\
 \quad \quad \quad \dots \dots \text{Quot.} \\
 \hline
 7978 \\
 15956 \\
 23934 \\
 3989 \\
 31912 \\
 \hline
 98204602 \text{ Proof.}
 \end{array}$$

The making of the little Table is easie, it being made by Addition only, thus; Having set down your Divisor 3989, double it, and

Recreations. 157

it is 7978, which set against the figure 2 ; then add them two numbers together, and they make 11967, which set against the figure 3 ; then to that number add 3989, & it makes 15956, which set against the figure 4 ; to this add still the first number (your divisor) 3989, and it will produce the Numbers as in the Table : and so must you do with any other Divisor.

And by this means *Multiplication* and *Division*, which are the two difficultest parts of *Arithmetick*, are easily and exactly performed by *Addition* and *Substraction*, without any charge to the memory.



Compendium 2.

In case a false Figure be placed in the Quotient of any Division, how to rectifie that Quotient without beginning the Work a-new.

WHen you have divided any Sum, if the Remainder at last be either greater or equal to the divisor, the quotient is false; which may be rectified without beginning the Work again, by dividing the Remainder only by the same divisor; for thereof will arise a new quotient, which added to the former quotient, the sum of them will be the true quotient.

So

Recreations. 159

- So if 7290 be divided by 27, the numbers being placed according to the usual way of Division.

Because 27 can be had in 72 but twice, set 2 in the quotient, saying 2 times 27 is 54, from 72, and there remains 18, which write over 72, 2
cancelling your other 59
figures: then say, How 2847
many times 27 in 7290 (259
189? say 7; but if you 2777
should mistake, and 22
write 5 in the Quo-
tient, and say 5 times 27 is 135,
out of 189, there remains 54,
which write down as before, and
remove the Divisor, & say, How
many times 27 in 540? the an-
swer is 20, but must never be a-
bove 9: say therefore 9 times 27
is 243, out of 540, and the re-
mainer is 297, which being the
last remain, (and greater than
H 2 the

160 *Arithmetical*

the Divisor) shewes the Work to be false, and the Quotient 359 to be too little.

Wherefore, divide the last remainder 297 by 27, and the quotient will be 11, and nothing remaining; wherefore, if you add this quotient 11, to the other quotient 259, the sum of them, 270, will be the true quotient of 7290 divided by 27.



Compen-

Compendium 3.

How to abbreviate your Work in Multiplication and Division, when your Multiplier or Divisor consist of a Unite with 1, 2, 3, or more Cyphers.

1. **T**Hus, if 365 were to be Multiplied by 10, add one Cypher thereunto, making it 3650, and it is done; if it were to be multiplied by 100, add 2 cyphers to it; if by 1000, add 3 cyphers to it, and your work is ended.

2. In Division likewise, if 763258 were to be divided by 10, cut off the last figure towards the right hand, and the rest of the figures is the quotient; so the quotient of 763258 divided by 10, is (76325⁸): if by 100, it
H 3
is

162 *Arithmetical*

is (7632 $\frac{18}{1000}$: if by 1000, it is (763 $\frac{258}{1000}$, &c.

3. Also if the Multiplier consist of one or more Cyphers in the last place, you may omit the multiplying of them, and set them down at last; as if it were required to multiply 3257 by 2600:

3257 2600 ——— 19542 6514 ——— 8468200	Place the numbers as you see here done: then multiply 3257 by 26, the product will be 84682; to which if you add two cyphers for the two cyphers in the Multi- plier, then it will be 8468200, which is the true pro- duct.
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4. Also if Cyphers be in the middle of the Multiplier among other figures, you may abbreviate your Work, by removing your next figure a place farther where any cypher comes. As

Recreations. 163

As if 682357 were to be multiplied by 30204 : Place the figures as is here done ;

$$\begin{array}{r}
 682357 \\
 30204 \\
 \hline
 2729428 \\
 1364714 \\
 2047071 \\
 \hline
 20609910828
 \end{array}$$

Then Multiply 682357 by 4, it produceth 2729428 ; then (because a cypher is next) skip one place, and multiply it by 2, it produceth 1364714, setting your 4 two places from your right hand towards the left : then for the next place, being a cypher, do the like, setting your multiplication by 3, namely 2047071, two places yet forwarder towards the left hand ; then add these

H 4 three

164 *Arithmetical*

three lines together, in the same order they now stand, and they make 20609910828, which is the true product of that multiplication.

Compendium 4.

How you may most compendiously and speedily multiply by any of the nine Digits, without charging of the Memory.

1. To Multiply any Number by 2.

Either double it, or set it down twice, and add the two sums together; but it is best done by doubling it in your mind.

So if you were to multiply 73684 by 2; it being set down once, begin at the right hand, and say, 4 and 4 is 8, set down 8; then 8 and 8 is 16, set down 6
and

Recreations. 165

and carry 1; then say 6 and 6 is 12, and 1 carried is 13, set down 3 and carry 1; then say 3 and 3 is 6, and 1 is 7, set down 7. Lastly, 7 and 7 is 14, which being the last figure, set 14 down, and your Multiplication is ended, and will stand thus:

147368.

II. To Multiply any Number by 3.

To the Number given, add the double thereof, the sum of them shall be the product.

So if you were to multiply 73684 by 3, first double it, or multiply it by 2, as before, and it maketh 147368, to which if you add the Given Number 73684, the sum of them will be 221052, which is equal to the product, as by the Work appears.

II 5

73684

166 *Arithmetical*

73684 Number given.
147368 its double.

221052 Multiplied by 3.

III. *To Multiply any Number by 4.*

Double the Duplication thereof, and your Work is ended.

So if you were to Multiply 73684 by 4, the Duplication thereof was 147368, which being doubled in your mind, or otherwise set down, giveth — 294736, which is the product of 73684 multiplied by 4, as here appeareth;

73684 Number given.
147368 its Duplication.

294736 Multiplied by 4.

IV. To

IV. *To Multiply any Number by 5.*

To the Number given add a Cypher, or in your mind conceive one to be added: the half of that number is the product thereof multiplied by 5.

So if you were to Multiply 73684 by 5, set, or conceive a cypher after the 4, then it is 736840; then beginning at the left hand, say, The half of 7 is 3, and 1 remaining: set down 3, and in your mind carry 1 to 3, making it 13: Then say, The half of 13 is 6, and 1 remaining; set down 6 and carry 1; then the half of 16 is 8, set down 8; then the half of 4 is 2, set down 2: lastly, the half of 0 is 0, set down 0, and your Work is ended; the product 4 being 368420, as by the work appears.

736840

168 *Arithmetical*

(cypher added.
736840 the number given, with a
368420 its Multiplication by 5.

V. *To Multiply any Number by 6.*

To the Number given add a cypher; then take the half of that number, and to it add the number given, the sum of them shall be the product of the given number multiplied by 6.

So if you were to Multiply 73684 by 6, add a cypher thereto, and it is 736840, the half whereof is 368420, to which if you add 73684 (the number given) the sum of them will be 442104, which is the product of 73684, being multiplied by 6. As here appeareth.

(cyph. added.
736840 the Number given, with a
368420 the half thereof.

73684

442104 the product mult. by 6.

VI. *To*

VI. To Multiply any Number by 7.

To the Number given add a cypher, & take the half thereof; add this half to the double of the number given, the sum thereof shall be the product of the given number multiplied by 7.

So if you were to Multiply 73684 by 7, add a cypher thereto, and it is 736840; the half of this number is 368420, which being added to 147368, the double of the given number, the sum will be 515788, which is the product of the given number 73684, being multiplied by 7: As here appeareth.

	(number.
147368	the double of the given
368420	half the given number, a
—	(cypher added.
515788	the product being multi-
	(plied by 7.

VII. T

VII. To multiply any Number by 8.

Double the Number given, and subtract that doubled number from the given number, a cypher being added thereto.

So if you were to Multiply 73684 by 8, the double of the given number is 147368; this being subtracted from 736540, (which is the given number with a cypher added) the remainder will be 589472, which is the product of the given number 73684, being multiplied by 8; as here appears.

(pher added.
736840 number given, with a cy-
147368 double of the giv. numb.

589472 product multiplied by 8.

VIII. To

VIII. To multiply any Number by 9.

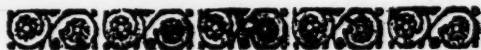
Add a Cypher to the given Number, and from that number subtract the given number, the remainder shall be the product.

So if you were to Multiply 73684 by 9, add a cypher to it, and it will be 736840; from which if you subtract 73684 your given number, the remainder will be 663156; which is the product of the given number Multiplied by 9: As here appeareth.

736840 given numb. with a cyph.

73684 the given number subtr.

663156 Product multiplied by 9.



Com-

 Compendium 5.

How readily to know how many Pounds are contained in any number of Shillings, without writing of them down, or troubling the Memory.

CONCEIVE the last figure of the Number given to be taken away, or cut off with a dash of the Pen; then the half of the other part of the Number are Pounds; and if 1 remain, that 1 is 10s. and the figure cut off (or supposed to be cut off) are shillings also.

Example.

In 642||7 Shillings, how many Pounds?

Suppose the 7 to be cut off; then the half of 6 is 3, set down 3; the half of 4 is 2, set down 2; the

Recreations. 173

the half of 2 is 1, set down 1: so
is there in 6427 shillings, 321 $l.$
7 $s.$

642||7 Shillings.
Pounds 321-7 Shillings.

In 579||8 Shillings, how many
Pounds?

Suppose the 8 to be cut off,
then say, The half of 5 is 2, and
1 remaining, set down 2 and car-
ry 1; then say, the half of 17
is 8, and 1 remaining, set down
8 and carry 1; then say, the half
of 19 is 9, and 1 remaining, set
down 9, which being your last
figure, the 1 remaining is 10 $s.$
which you must add to the 8
that was cut off, and it makes
18 $s.$ So that in 5798 shillings
there are 289 $l.$ —18 $s.$ As here ap-
peareth.

xx (1 $s.$
579|| 8 Shillings.
289 Pounds—18 $s.$

If

174 *Arithmetical*

If you would turn Pounds at one work into Pence, then Multiply the Pounds by 140, and the product is Pence.

So 235 *l.* being multiplied by 240, produceth 56300 pence.

On the contrary, to bring Pence into Pounds at one work, divide the Pence by 240, and the quotient will be Pounds.

So 56300 Pence being divided by 240, produceth in the quotient 235 *l.*



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Compendium 6.

When any Question is propounded in the Rule of Three, where Halves, Quarters, or three Quarters of Weight or Measure are in the Question, or where Nine-pences, Six-pences, or Three-pences are ingredients, how you shall resolve such Questions without the help of Fractions, or reducing of your Money, Weight, Measure, to their least Denomination.

YOU must here suppose your Money, Weight, or Measure, the Integer to be divided into 100 parts; which being presupposed, the 25 is a Quarter, 50 is Half, and 75 is three Quarters of any Money, Weight, or Measure.

This

176 *Arithmetical*

This presupposed, we will proceed to *Example 1.*

If 3 yards of anything cost 1 s. 3 d.
what will 85 yards cost ?

$$\begin{array}{r}
 3 \text{ ————— } 11.25 \text{ ————— } 85 \\
 \phantom{3 \text{ ————— } } 85 \\
 \hline
 \phantom{3 \text{ ————— } } 5625 \\
 \phantom{3 \text{ ————— } } 9000 \\
 \hline
 \phantom{3 \text{ ————— } } 956.25
 \end{array}$$

l. s. d.
15—18—9

221
85825 (31 || 8.75
33333

Here

Recreations. 177

Here instead of 11 s.—3 d. I set down 11.25, the 11 signifying 11 s. and the 25 3 d. which is the quarter of a shilling; and then I multiply and divide, as if it were all whole numbers. For multiplying 11.25 by 85, the product is 956.25; the 25 at the end separated by a prick, is the fraction of a quarter. This number divided by 3, the quotient is 318.75, that is, 318 s. and 75, that is three quarters of a shilling, or 9 d. So that if 3 yards cost 11 s.—3 d. 85 yards will cost 18 s. and 9 d. which is 15 l.—18 s. 9 d.

Example

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Example 2.

If $6\frac{1}{2}$ Ells of any Commodity cost
12 l. - 15 s. what shall $37\frac{1}{4}$ Ells
cost ?

Set your numbers thus :

Ells.	l.	Ells.
If 6.50—cost—	12.75—	what—37.25
		12.75
		<hr/>
		18625
		26075
		7450
		3725
		<hr/>
xx 4		
3047		
4740375	(73.06	4749375
688550		
666		

Here instead of 6 Ells and $\frac{1}{2}$,
set down 6.50, 50 being the half
of 100. Again, for 12 l. - 15 s.
set down 12.75, 75 being three
quarters of 100, as 15 s. is $\frac{3}{4}$ of a
Pound. And lastly, for 37 Ells
and

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and a quarter, I set down 37.25,
25 being one quarter of 100.

And then multiplying and di-
viding of these as whole Num-
bers, according to the nature of
working the *Rule of Three*, I find
my quotient to come out 73.06,
that is, 73 $l.$ $\frac{6}{100}$ parts of a pound,
or 20 $s.$ which reduced, is 1 $s.$ 2 $d.$
1 $q.$ $\frac{6}{10}$ of a farthing. So that if
6 $\frac{1}{2}$ Ells cost 12 $l.$ 15 $s.$ 37 $\frac{1}{4}$ Ells
will cost 73 $l.$ 1 $s.$ 2 $d.$ 1 $q.$ $\frac{6}{10}$.



F I N ! S.

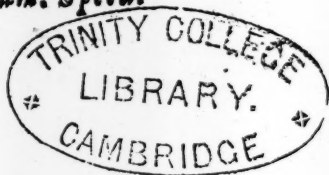


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